# **Tutorial for Harmonic Analysis using CAEPIPE**

#### The following are the Steps to perform Harmonic Analysis using CAEPIPE.

#### General

 A harmonic analysis is performed to determine the response of a piping system to sinusoidal loads. Harmonic forces can arise from unbalanced rotating equipment, acoustic vibrations caused by reciprocating equipment, flow impedance, and other sources. These forces can be damaging to a piping system if their frequency is close to the piping system's natural frequency, thereby introducing resonant conditions.

It is feasible that multiple harmonic loads may be applied simultaneously at different locations of a piping system. More complex forms of vibration, such as those caused by the fluid flow, may be considered as superposition of several simple harmonics, each with its own frequency, magnitude, and phase.

• A harmonic analysis uses the results from the modal analysis to obtain a solution. A single damping factor is used for all modes.

First, the maximum response for each harmonic load is obtained separately. Then, the total response for multiple simultaneous harmonic loads is determined by combining the individual responses. The combination method may be specified as the Root Mean Square (RMS) or Absolute Sum. Even in the case of a system with a single harmonic load, the said combination is always carried out, so that the resulting solution becomes an "unsigned" case. For an unsigned case, the actual values for displacements, element forces and moments, etc. computed internally by CAEPIPE prior to such combination can be +ve or -ve for the dynamic event.

#### Step 1:

Attached is a CAEPIPE model for Harmonic Analysis. For this model, let us assume the following.

- 1. Node 5 is connected to a Tank.
- 2. Node 40 is connected to a Pump Suction Nozzle.



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|----------|-------------------|-------------|------------------------|---------------|---------------|---------------------|-------------|-----------------|------------------|------------------|----------------|-------------|------------------|-------------------|--------------------|------|
| File     | Edit Viev         | v Optior    | ns Misc                | Window        | Help          |                     |             |                 |                  |                  |                |             |                  |                   |                    |      |
| +        |                   |             | )] Q                   | н             | <b>(</b> 2    |                     |             | •               |                  |                  |                |             |                  |                   |                    |      |
| #        | Name              | Descript    | ion                    |               |               | Density<br>(lb/in3) | Nu          | Joint<br>factor | Yield<br>(psi)   | Tensile<br>(psi) | : #            | Temp<br>(F) | E<br>(psi)       | Alpha<br>(in/in/F | Allowat<br>) (psi) | ole  |
| 1        | 312               | A312 TP     | <mark>316 (16</mark> 0 | Dr-12Ni-2Mo   | ) AS          | 0.289               | 0.3         | 1.00            |                  |                  | 1              | -325        | 30.3E+6          | 8.15E-6           | 5 20000            |      |
| 2        |                   |             |                        |               |               |                     |             |                 |                  |                  | 2              | -200        | 29.7E+6          | 8.47E-6           | 5 20000            | _ '  |
|          |                   |             |                        |               |               |                     |             |                 |                  |                  | 3              | -100        | 29.0E+6          |                   |                    | - 11 |
|          |                   |             |                        |               |               |                     |             |                 |                  |                  | 4              | 70          | 28.3E+6          |                   |                    | - 1  |
|          |                   |             |                        |               |               |                     |             |                 |                  |                  | 5              | 200         | 27.6E+6          |                   |                    | _ 1  |
|          |                   |             |                        |               |               |                     |             |                 |                  |                  | 6              | 300         | 27.0E+6          |                   |                    | - 1  |
|          |                   |             |                        |               |               |                     |             |                 |                  |                  | 7              | 400         | 26.5E+6          |                   |                    | - 1  |
|          |                   |             |                        |               |               |                     |             |                 |                  |                  | 8              | 500         | 25.8E+6          |                   |                    |      |
|          |                   |             |                        |               |               |                     |             |                 |                  |                  | 9              | 600         | 25.3E+6          | 9.82E-6           | 6 17000            |      |
| File     | Edit              | View        |                        | is Misc       | Wind          |                     | Help        | -               | ->               |                  |                |             |                  |                   |                    |      |
| #        | Name              | Nom<br>Dia  | Sch                    | OD<br>(inch)  | Thk<br>(inch  | Cor.<br>) (incl     |             | M.Tol<br>(%)    | Ins.D<br>(Ib/ft3 |                  | ns.Tl<br>inch) |             | n.Dens<br>)/ft3) | Lin.T             |                    |      |
| 1        | 6                 | 6"          | STD                    | 6.6248        | 0.28          |                     | Í           | . ,             | 11               | · ·              | .559           |             | . ,              |                   | ,<br>              |      |
| 2        | 8                 | 8"          | STD                    | 8.6248        | 0.322         |                     |             |                 |                  |                  |                |             |                  |                   |                    |      |
| 3        | 10                | 10"         | STD                    | 10.75         | 0.365         | _                   | _           |                 |                  |                  |                |             |                  |                   |                    |      |
|          |                   | ·-          |                        | 1             |               |                     |             |                 |                  |                  |                |             |                  | I                 |                    | _    |
|          |                   |             |                        | [harmoni      | -             |                     | -           |                 | ls\harm          | nonican          | alysis         | 5)]         |                  | _                 |                    | ×    |
| File     | Edit              | View        | Option                 | is Misc       | Wind          | 1 wor               | Help        |                 |                  |                  |                |             |                  |                   |                    |      |
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| #        | Name              | T1<br>(F)   | P1<br>(psi)            | Desg.T<br>(F) | Desi<br>(psi) |                     | Spe<br>grav |                 | Add.W<br>Ib/ft)  | ~ .              | 'ind<br>bad 1  | Win<br>Loa  |                  | /ind<br>bad 3     | Wind<br>Load 4     |      |
| 1        | <u>_</u> 1        | 365         | 145                    | 365           | 145           |                     | 1.0         |                 |                  |                  |                |             |                  |                   |                    |      |
| 2        | L2                | 500         | 464                    | 500           | 464           |                     | 1.0         |                 |                  |                  |                |             |                  |                   |                    |      |
| <u> </u> |                   | 1.00        |                        |               | 1.2.          |                     |             |                 |                  |                  |                |             |                  |                   |                    |      |

## Step 2:

The harmonic load can be imposed as a Force (FX/FY/FZ) at a specified frequency and phase angle. You may be able to get more information on the harmonic loading (mass, rpm, etc.) from the manufacturer of the equipment.

For this Tutorial, the following assumptions are made.

- 1. Frequency of the rotating equipment = 14.5 Hz.
- 2. Force in Global Z Direction = FZ = 9000 lb.

The above parameters are entered for analysis by creating a "Data" type called "Harmonic Load" through Layout window > Misc > Data types... at Node 40. See snap shot below for details.

| Harmonic load at node 40 | ×               |
|--------------------------|-----------------|
| Frequency 14.5           | (Hz)            |
| Phase                    | (deg)           |
| FX (lb) FY (lb)          | FZ (lb)<br>9000 |
| OK Cancel                |                 |

#### Step 3:

Define "Percentage of Damping" and "Combination" method for Harmonic analysis through CAEPIPE Layout window > Loads > Harmonic...

| Harmonic Analysis $	imes$                           |
|---|
| Damping 🚺 (%)                                       |
| Combination<br>C Root Mean Square<br>C Absolute Sum |
| OK Cancel   |

#### Step 4:

Then, include "Harmonic response" for analysis through Layout window > Loads > Load cases.

## Step 5:

Save the model and perform the analysis through Layout window > File > Analyze. CAEPIPE will apply these loads to compute the response of the piping system by performing a Harmonic analysis along with other load cases defined in the piping system.

#### Step 6:

Upon successful analysis, CAEPIPE will now show a "Load case" with name "Harmonic response" under "Support Loads", "Displacements", "Element forces" and "Support load summary" results.

| Load cases (5)        | ×                   |  |  |  |  |
|-----------------------|---------------------|--|--|--|--|
| ☑ Sustained (W+P)     | 🔲 Design (W+PD+TD)  |  |  |  |  |
| Empty Weight (W)      | 🔽 Modal analysis    |  |  |  |  |
| 💌 Expansion (T1)      | ✓ Harmonic response |  |  |  |  |
| 🔽 Operating (W+P1+T1) |                     |  |  |  |  |
| OK Cancel             | All None            |  |  |  |  |

| -0     | ' Caepi   | ipe : Lo     | ads on             | Anchor              | s: Harmo               | nic resp     | onse -               | [harmon              | icanalysi             | is.res           | (c:\tuto      | ials         |       | _                       |                         | ×                    |
|--------|-----------|--------------|--------------------|---------------------|------------------------|--------------|----------------------|----------------------|-----------------------|------------------|---------------|--------------|-------|-------------------------|-------------------------|----------------------|
| Fil    | e Res     | ults \       | liew               | Options             | Windo                  | w Hel        | р                    |                      |                       |                  |               |              |       |                         |                         |                      |
| 4      | 3         | + (          |                    |                     | ið (                   | 2            |                      |                      | ⇒                     | $\equiv$         | 🔶             |              |       | Ī                       | 4                       |                      |
| #      | Nod       | e Ta         | a FX               | (lb)                | FY (lb)                | FZ (I        | b)                   | MX (ft-lb)           | MY (f                 | ft-lb)           | MZ (ft-       | lb)          |       |                         |                         |                      |
| 1      | 5         |              | 396                | • •                 | 16                     | 217          | ,                    | 62                   | 2591                  |                  | 2870          | ,            |       |                         |                         |                      |
| 2      | 40        |              | 533                |                     | 1493                   | 2            |                      | 166                  | 3418                  |                  | 7354          |              |       |                         |                         |                      |
| 3      | 125       |              | 32                 |                     | 64                     | 48           |                      | 315                  | 235                   | •                | 143           |              |       |                         |                         |                      |
| Ľ      |           |              | 1                  |                     |                        | 1            |                      |                      | 1                     |                  |               |              |       |                         |                         |                      |
| 1-0-   | Caepip    | e : Disp     | laceme             | nts: Harm           | ionic respo            | onse - [h    | armoni               | canalysis.re         | s (c:\tuto            | orials∖h         | armonic       | analy        | sis)] |                         |                         | ×                    |
| File   | e Resul   | lts Vie      | w Op               | tions V             | Vindow I               | Help         |                      |                      |                       |                  |               |              |       |                         |                         |                      |
| 4      | 3   -     | ┢            |                    |                     | )                      |              |                      | -                    |                       | (-               | →             | 1            | 4     | ∍ ⊏                     | >                       | <b>—</b> A           |
| #      |           |              |                    | [                   | Displacer              | ments (g     | (lobal)              |                      |                       |                  |               |              |       |                         |                         |                      |
|        |           | X (inc       |                    | ′ (inch)            | Z (inch)               | XX (c        |                      |                      | ZZ (deg               | 3)               |               |              |       |                         |                         |                      |
| 1      | 5         | 0.000        |                    | .000                | 0.000                  | 0.000        | -                    |                      | 0.0000                |                  |               |              |       |                         |                         |                      |
| 2      | 10        | 2.844        |                    | .000                | 0.000                  | 0.000        |                      |                      | 0.0812                | -11              |               |              |       |                         |                         |                      |
| 3      | 15A       | 0.333        |                    | .005                | 0.000                  | 0.008        |                      |                      | 0.1675                | -11              |               |              |       |                         |                         |                      |
| 4      | 15B       | 0.845        |                    | .010                | 0.007                  | 0.034        |                      |                      | 0.0566                | - 4              |               |              |       |                         |                         |                      |
| 5      | 20A       | 0.053        |                    | .009                | 0.071                  | 0.035        |                      |                      | 0.2405                | - 1              |               |              |       |                         |                         |                      |
| 6<br>7 | 20B<br>45 | 0.000        |                    | .033<br>.120        | 0.073                  | 0.074        |                      |                      | 0.1035<br>0.0381      | - 1              |               |              |       |                         |                         |                      |
| 8      | 25        | 0.000        |                    | .120                | 0.237                  | 0.007        |                      |                      | 0.0381                | -                |               |              |       |                         |                         |                      |
| 9      | 50        | 0.000        |                    | .105                | 0.158                  | 0.007        |                      |                      | 0.0381                | - 1              |               |              |       |                         |                         |                      |
| 10     | 30        | 0.000        |                    | .103                | 0.135                  | 0.007        |                      |                      | 0.0415                | -                |               |              |       |                         |                         |                      |
| 11     | 35        | 0.000        |                    | .083                | 0.025                  | 0.000        |                      |                      | 0.0603                | - 1              |               |              |       |                         |                         |                      |
| 12     | 38        | 0.000        |                    | .001                | 0.404                  | 0.000        |                      |                      | 0.0140                | - 1              |               |              |       |                         |                         |                      |
| 13     | 40        | 0.000        |                    | .000                | 0.407                  | 0.000        |                      |                      | 0.0000                |                  |               |              |       |                         |                         |                      |
|        | 1         | 0.000        |                    | 110                 | 0.100                  | 0.045        | - <u> </u>           | 0.01.70              | 0.0001                |                  |               |              |       |                         |                         |                      |
| HIH    | Caepipe : | Pipe forc    | es in loca         | al coordina         | tes: Harmoni           | c response   | - [harm              | onicanalysis.r       | es (c:\tutor          | rials\har        | monicanal     | ysis)]       |       |                         | - 1                     | - ×                  |
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| 8      |           |              |                    | <u>ið</u> i 6       | 1                      |              |                      | <b>■ ←</b> •         |                       |                  |               |              |       | I                       |                         |                      |
| #      |           | lb)          | y Sheaı<br>(lb)    | r z Shear<br>(lb)   | Torsio<br>Moment       | <u> </u>     | Inpla<br>Momei       | ane(ft-lb)<br>nt SIF | Outpla<br>Moment      | ne(ft-lb)<br>SIF | ) Fle:<br>FFi | < Fac<br>FFo |       | SL+SO<br>(psi)          | (psi)                   | SL+SO                |
| 1      |           | 217<br>217   | 16<br>16           | 39600<br>39600      | 2870<br>2870           |              | 62<br>128            |                      | 259143<br>216060      |                  |               |              |       | 105765<br>90279         | 25995<br>25995          | 4.07<br>3.47         |
| 2      |           | 248<br>248   | 82<br>82           | 17395<br>17395      | 2870<br>2870           |              | 128<br>920           |                      | 216060<br>5728        |                  |               |              |       | 90281<br>4114           | 25995<br>25995          | 3.47<br>0.16         |
| 3      | 15A 2     | 283          | 176                | 13490               | 2870                   | 1.00         | 920                  | 2.54                 | 5728                  | 2.12             | 7.95          | 7.95         |       | 5896                    | 25995                   | 0.23                 |
| 4      | 15B 3     | 176<br>307   | 283<br>911         | 13490<br>299        | 22590<br>22590         | 1.00         | 787                  | 2.54                 | 13992<br>787          | 2.12             | 7.95          | 7.95         |       | 14704<br>12175          | 25995<br>25995          | 0.57                 |
| 5      | 20A 4     | 307<br>431   | 911<br>1659<br>431 | 299<br>1567<br>1567 | 22590<br>22590<br>2928 | 1.00         | 3320<br>3320<br>5932 | 2.54<br>2.54         | 4887<br>4887<br>24549 | 2.12<br>2.12     | 7.95<br>7.95  | 7.95         |       | 10815<br>11643<br>18384 | 25995<br>25995<br>25995 | 0.42<br>0.45<br>0.71 |
| 6      | 20B 1     | 1659<br>1627 | 431<br>110         | 1567<br>226         | 2928<br>2928           | 1.00         | 5932                 | 2.54                 | 24549<br>24549        | 2.12             | 7.95          | 7.95         |       | 11821                   | 25995<br>25995          | 0.45                 |
| 7      | 45 1      | 1627<br>1599 | 110<br>1042        | 226<br>3284         | 2928<br>2928           | 1.00         | 7239                 |                      | 27228                 | 1.00             |               |              |       | 13165<br>13162          | 25995<br>25995          | 0.51                 |
| 8      | 25 5      | 1599<br>517  | 1042<br>883        | 3284<br>8919        | 2928<br>166            | 1.39<br>1.39 | -24286<br>-40390     | 2.00<br>2.00         | 6306<br>6176          | 1.00             |               |              |       | 16800<br>26199          | 25995<br>25995          | 0.65                 |
|        | 50 15     | 517 I        | 883                | 8919                | 1166                   |              | 5385                 |                      | 32400                 |                  | 1             |              |       | 14779                   | 25995                   | 1057                 |

| =1= Caepipe : Support load summary for anchor at node 5 - [harmonicanalysis.res (c: $ \Box$ $	imes$ |         |         |         |            |            |            |  |  |  |  |
|---|---------|---------|---------|------------|------------|------------|--|--|--|--|
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| $\textcircled{\begin{tabular}{ c c c c } \hline @ & @ & @ & @ & @ & @ & @ & & & & & &$              |         |         |         |            |            |            |  |  |  |  |
| Load combination  | FX (lb) | FY (lb) | FZ (lb) | MX (ft-lb) | MY (ft-lb) | MZ (ft-lb) |  |  |  |  |
| Sustained   | -24     | 233     | -98     | -1783      | -871       | -185       |  |  |  |  |
| Operating1  | 195     | 799     | -106    | -3998      | 4147       | -2077      |  |  |  |  |
| Sustained+Harmonic  | 39576   | 249     | 120     | -1721      | 258271     | 2685       |  |  |  |  |
| Sustained-Harmonic  | -39624  | 218     | -315    | -1845      | -260014    | -3056      |  |  |  |  |
| Operating1+Harmonic   | 39795   | 814     | 111     | -3936      | 263289     | 793        |  |  |  |  |
| Operating1-Harmonic   | -39406  | 783     | -324    | -4060      | -254996    | -4948      |  |  |  |  |
| Maximum   | 39795   | 814     | 120     | -1721      | 263289     | 2685       |  |  |  |  |
| Minimum   | -39624  | 218     | -324    | -4060      | -260014    | -4948      |  |  |  |  |
| Allowables  | 0       | 0       | 0       | 0          | 0          | 0          |  |  |  |  |
| J   |         |         |         |            |            |            |  |  |  |  |

# Step 7:

From the review of frequency results of CAEPIPE, it is noted that one of the natural frequencies of this piping system (i.e., frequency for Mode 10 shown in yellow highlight in the snap shot below) is close to the rotating equipment frequency of 14.5 Hz.

| -0-1 | 🍽 Caepipe : Frequencies - [harmonicanalysis.res (c:\tutorials\harmonicanalysi — 🛛 🛛 🛛 |          |         |            |         |        |          |          |  |  |  |
|------|---|----------|---------|------------|---------|--------|----------|----------|--|--|--|
| File | File Results View Options Window Help   |          |         |            |         |        |          |          |  |  |  |
| 4    |   |          |         |            |         |        |          |          |  |  |  |
| #    | Frequency   | Period   |         | ipation fa | actors  |        | nass/Tot | tal mass |  |  |  |
|      | (Hz)  | (second) | ×       | Y          | Z       | ×      | Y        | Z        |  |  |  |
| 1    | 1.473   | 0.6788   | 0.0528  | 0.5034     | -3.3441 | 0.0001 | 0.0130   | 0.5743   |  |  |  |
| 2    | 2.502   | 0.3998   | -1.4706 | -0.6359    | -0.1343 | 0.1111 | 0.0208   | 0.0009   |  |  |  |
| 3    | 3.141   | 0.3184   | -2.4648 | 0.5853     | 0.0084  | 0.3120 | 0.0176   | 0.0000   |  |  |  |
| 4    | 3.702   | 0.2702   | 0.2151  | 3.1984     | 0.3743  | 0.0024 | 0.5254   | 0.0072   |  |  |  |
| 5    | 3.763   | 0.2657   | 0.1984  | 1.1702     | 0.1233  | 0.0020 | 0.0703   | 0.0008   |  |  |  |
| 6    | 5.048   | 0.1981   | -0.1425 | 0.3283     | 0.1984  | 0.0010 | 0.0055   | 0.0020   |  |  |  |
| 7    | 5.539   | 0.1805   | -0.0228 | -0.0144    | -0.7486 | 0.0000 | 0.0000   | 0.0288   |  |  |  |
| 8    | 5.901   | 0.1695   | 0.1759  | 0.0126     | 0.1174  | 0.0016 | 0.0000   | 0.0007   |  |  |  |
| 9    | 8.568   | 0.1167   | -1.3319 | 0.0917     | 0.0886  | 0.0911 | 0.0004   | 0.0004   |  |  |  |
| 10   | 14.553  | 0.0687   | -1.0193 | -0.0477    | -0.0036 | 0.0534 | 0.0001   | 0.0000   |  |  |  |
| 11   | 16.917  | 0.0591   | 0.1139  | -0.9348    | -0.0311 | 0.0007 | 0.0449   | 0.0000   |  |  |  |
| 12   | 27.478  | 0.0364   | -0.0830 | -0.0110    | -0.0420 | 0.0004 | 0.0000   | 0.0001   |  |  |  |
| 13   | 51.942  | 0.0193   | 0.3711  | -0.0917    | -0.7651 | 0.0071 | 0.0004   | 0.0301   |  |  |  |
| 14   |   |          |         |            | Total   | 0.5828 | 0.6985   | 0.6454   |  |  |  |
|      |   |          |         |            |         |        |          |          |  |  |  |

Due to closeness of Mode 10 frequency to the equipment frequency, it is observed that Mode 10 is excited on the piping system by the harmonic load, thereby creating a resonance. This can be seen graphically by plotting the mode shape corresponding to Mode 10 with frequency of "14.55 Hz" (figure shown on the left below) and the deflected shape for "harmonic response" case (figure shown on the right below). See snap shots for details.



#### Step 8:

In order to prevent piping failure due to resonance, it is important to suppress relevant modes by changing the stiffness of the piping system either by adding or by moving the existing piping supports. For example, for the layout shown above, a lateral restraint in X direction is added at Node 10 as the displacement in X direction is about 3" for Harmonic Response case prior to adding this X restraint. By adding this new support, the stiffness of the piping system is altered. This, in turn, removed the 10<sup>th</sup> frequency with "14.55 Hz", thereby ensuring that the natural frequency of the piping system is not close to the operating equipment frequency. See snap shots below.



| 1-0-1 | 📲 Caepipe : Frequencies - [harmonicanalysis_trx_10.res (c:\tutorials\harmoni — 🛛 🛛 🛛 |          |         |            |         |        |          |          |  |  |  |
|-------|--|----------|---------|------------|---------|--------|----------|----------|--|--|--|
| File  | File Results View Options Window Help  |          |         |            |         |        |          |          |  |  |  |
| Æ     |  |          |         |            |         |        |          |          |  |  |  |
| #     | Frequency  | Period   |         | ipation fa | actors  |        | nass/Tot | tal mass |  |  |  |
|       | (Hz)   | (second) | ×       | Y          | Z       | ×      | Y        | Z        |  |  |  |
| 1     | 1.474  | 0.6783   | -0.0075 | -0.4970    | 3.3457  | 0.0000 | 0.0127   | 0.5749   |  |  |  |
| 2     | 2.956  | 0.3382   | -0.9955 | 0.9922     | 0.0814  | 0.0509 | 0.0506   | 0.0003   |  |  |  |
| 3     | 3.581  | 0.2792   | -1.5073 | -1.3860    | -0.1892 | 0.1167 | 0.0987   | 0.0018   |  |  |  |
| 4     | 3.729  | 0.2682   | 0.0054  | 3.0516     | 0.3445  | 0.0000 | 0.4782   | 0.0061   |  |  |  |
| 5     | 4.705  | 0.2125   | -1.8744 | 0.4453     | 0.0945  | 0.1804 | 0.0102   | 0.0005   |  |  |  |
| 6     | 5.101  | 0.1961   | -0.4923 | -0.2136    | -0.1835 | 0.0124 | 0.0023   | 0.0017   |  |  |  |
| 7     | 5.540  | 0.1805   | 0.0155  | -0.0171    | -0.7481 | 0.0000 | 0.0000   | 0.0287   |  |  |  |
| 8     | 5.904  | 0.1694   | -0.2497 | -0.0065    | -0.1154 | 0.0032 | 0.0000   | 0.0007   |  |  |  |
| 9     | 8.585  | 0.1165   | -1.3138 | 0.0878     | 0.0881  | 0.0886 | 0.0004   | 0.0004   |  |  |  |
| 10    | 16.913   | 0.0591   | -0.0654 | 0.9358     | 0.0313  | 0.0002 | 0.0450   | 0.0001   |  |  |  |
| 11    | 27.472   | 0.0364   | -0.1185 | -0.0109    | -0.0420 | 0.0007 | 0.0000   | 0.0001   |  |  |  |
| 12    | 51.938   | 0.0193   | 0.3657  | -0.0902    | -0.7605 | 0.0069 | 0.0004   | 0.0297   |  |  |  |
| 13    |  |          |         |            | Total   | 0.4601 | 0.6985   | 0.6450   |  |  |  |
|       |  |          |         |            |         |        |          |          |  |  |  |
|       |  |          |         |            |         |        |          |          |  |  |  |